## MATH 3341 — Spring 2021

## Lab 12: Romberg Integration

If you haven't downloaded and unzipped Math.3341.zip. Download and unzip it under H: (H Drive if you are working on the Remote Lab). Change the current working directory by typing cd H:\Math.3341\Math.3341.Lab.12 in the Command Window, and type edit lab\_12\_script in the Command Window to edit lab\_12\_script.m.

- 1. Download the file Math.3341.Lab.12.zip, un-zip it.
- 2. The algorithm for Romberg integration is given below (see Algorithm 1). Please implement the algorithm in MATLAB in the provided function file lab\_12\_romberg.m.

**Algorithm 1:** Romberg integration: approximates  $I = \int_a^b f(x) dx$  using n intervals.

```
Function romberg(f, a, b, n):

Input: f is the integrand, a is the lower bound, b is the upper bound, n is the number of subintervals.

Output: The integral of f(x) over the interval [a, b] using 1, 2, 3, \ldots, n subintervals. h \leftarrow b - a;

R_{1,1} \leftarrow [f(a) + f(b)] \cdot h/2;

for k \leftarrow 2 to n do

R_{k,1} \leftarrow \frac{1}{2} \left[ R_{k-1,1} + h \sum_{j=1}^{2^{k-2}} f(a + (2j-1) \cdot h/2) \right];

for j \leftarrow 2 to k do

R_{k,j} \leftarrow R_{k,j-1} + \frac{R_{k,j-1} - R_{k-1,j-1}}{4^{j-1} - 1};

end
h \leftarrow h/2;
end
return [R_{1,1}, R_{2,2}, R_{3,3}, \ldots, R_{n,n}];
```

- 3. Run the script file lab\_12\_script.m to verify your function is working.
- 4. Uncomment line 18 through line 52 in the script file lab\_12\_script.m, and add more test functions to lab\_12\_script.m:

(a) 
$$\int_0^\pi x^3 \sin x \, dx.$$

(b) 
$$\int_1^5 x^3 (\ln x)^2 dx$$
.

(c) 
$$\int_{e^e}^{e^4} \ln \ln \ln x \, dx.$$

5. Add plots for Romberg integration error of test functions g(x), h(x), p(x) against n, which are also indicated in the comments (around line 65 through line 69).

- 6. Run diary('lab\_12\_output.txt'), run the script file lab\_12\_script.m, then call diary off to save the output to the specified text file.
- 7. Upload lab\_12\_output.txt, lab\_12\_figure.pdf, lab\_12\_script.m, and lab\_12\_romberg.m to Overleaf, recompile and submit the .pdf report to WyoCourses.