MATH 3341 — Fall 2020

Lab 13: Random Numbers, Histogram & Monte Carlo Integration

Download Math.3341.Lab.13.zip, unzip it and replace the files under H:\Math.3341\Math.3341.Lab.13. Change the current working directory by typing cd H:\Math.3341\Math.3341.Lab.13 in the Command Window, and type edit lab_13_script in the Command Window to edit lab_13_script.m.

1 RANDOM NUMBERS AND HISTOGRAM

- (a) Create a vector \mathbf{x} _uniform of length N=10000 random numbers, which are uniformly distributed on the interval [-3.5, 3.5], using rand.
- (b) Create a vector x_normal of length N=10000 random numbers, which are normally distributed with zero mean $\mu=0$ and unit variance $\sigma^2=1$, using randn.
- (c) Create historgrams for x_uniform and x_normal.

2 Monte Carlo Integration

- (a) Open lab_13_example.m and monteCarlo.m. Go through lab_13_example.m, see how the script is written to use Monte Carlo Integration to integrate the function f(x,y)=1 over the disk $x^2+y^2\leq 1$. Then convert the Monte Carlo Integration part in the script to a function in monteCarlo.m.
- (b) Then in lab_13_script.m, use monteCarlo.m to evaluate the following integral using N=100000 samples:

$$\int_{-1}^{1} \int_{2x^2}^{1+x^2} (x+2y) \, dy \, dx.$$

(c) Use the built-in function integral 2 to evaluate the above integral, and compare the error between these two integrations.

Finally, call diary('lab_13_output.txt'), run the script lab_13_script.m, and then call diary off to save the output. Upload the script file lab_13_script.m, function file monteCarlo.m, figure file lab_13_figure.pdf, and output file lab_13_output.txt to Overleaf. Recompile, and submit the generated .pdf file on WyoCourses.